

Index

- Abel's series 76, 156
- absolute convergence
 - of series 45
 - of singular integrals 148
- absolute value 7
- addition formulae for sine and cosine 84
- alternating series test 46
- Archimedean axiom 13
- arithmetic of limits
 - of sequences 21
 - of functions 62
- arithmetic mean 35, 56
- axiom 1

- Bernoulli's inequality 7, 108, 119
- binomial theorem 119
- Bolzano–Weierstrass theorem 32
- boundedness
 - of set 10
 - of sequence 20
 - of function 88

- Cauchy's mean value theorem 110
- Cauchy product 54
- closed interval 10
- common refinement 124
- commutative law 51
- comparison test
 - for series 42, 43
 - for singular integrals 146
- composition
 - of continuous functions 70
 - of differentiable functions 97
- condensation test 56
- conditional convergence
 - of series 47, 51
 - of singular integrals 149
- continuity 69
- convergence
 - of sequences 18
 - of series 37
 - of singular integrals 142, 144
- curve sketching 108

- Darboux' theorem 132
- decimal expansion 55
- decreasing function 73
- decreasing sequence 29
- definite integral 125
- density of rationals 14
- derivative 93, 95, 112
- differentiability 93, 95, 112
- Dirichlet's function 126
- discontinuity 68
- dissection 122
- distributive law 51
- divergence
 - of sequences 25
 - of series 37
 - of functions 65
 - of singular integrals 143, 144

- e
 - definition of 31, 79
 - irrationality of 120
- Euler's limit 152
- Euler's series 39, 156
- even subsequence 31
- exponential function
 - definition and basic properties of 79–81
 - differentiability of 105
- exponential theorem 79

- factorial function 150
- function 59
- fundamental theorem of calculus
 - statement of 121
 - proof of 132, 136

- gamma function 151
- geometric mean 35
- geometric sequence 24, 28
- geometric series 38, 41
- graph 5, 68, 92, 109, 121
- greatest lower bound 13

- harmonic mean 35, 36
- harmonic series 38
- higher derivatives 112

- increasing function 73
- increasing sequence 29

- indefinite integral 106
- induction 2, 15
- inequalities 2–9
- infimum 13
- infinite differentiability 112
- integrability
 - definition of 125
 - of monotonic functions 127
 - of continuous functions 128
- integral test for series 151
- integrand 139
- integration
 - of inequalities 134
 - by parts 137
 - by substitution 138
- intermediate value theorem 72
- interval 10
- interval additivity of the integral 135
- interval of convergence of a power series 113
- inverse function 71
- inverse function theorem
 - for continuous functions 74
 - for differentiable functions 100
- irrational number 2
- irrational powers 80, 82
- irrationality
 - of $\sqrt{2}$ 2
 - of e 120
- laws
 - of indices 83
 - of inequalities 3
 - of logarithms 83
- least upper bound 11
- left-hand derivative 95
- Leibnitz notation 92
- l'Hopital's rule 111
- limit
 - of sequence 18
 - of function 59
 - one-sided 63
- linear combination
 - of series 40
 - of integrals 133
- logarithms
 - definition and basic properties of 81–3
 - differentiability of 105
- lower bound 10
- lower integral 125
- lower sum 122
- Machin's formula 120
- Maclaurin series 113
- mathematical induction 2, 15
- maximum 10
- mean value theorem
 - of differential calculus 102
 - Cauchy's 110
 - nth 116
 - of integral calculus 141
- minimax theorem 88
- minimum 10
- modular inequality
 - for series 57
 - for integrals 134
- modulus
 - of a number 7
 - of a dissection 130
- monotonicity
 - of a sequence 29
 - of a function 73
- multiplication of series 53
- nested sequence of intervals 33
- Newton's method for square roots 35
- non-null test 42
- nth mean value theorem 116
- nth roots 75, 101
- nth root test 56
- null sequence 19
- odd subsequence 32
- open interval 10
- open sandwich principle 27
- ordinary integral 142
- oscillation
 - of sequence 26
 - of series 37
- partial sum 37
- periodicity 86
- π
 - definition of 86
 - calculation of 120
- polynomial 70
- power series 48
- primitive 106
- proof of inequalities using calculus 109
- radius of convergence 49
- ratio test 44
- rational number 1
- rational function 70
- real line 1
- real number 1
- rearrangement of series 51
- refinement of a dissection 123
- Riemann's condition 127
- Riemann sum 132
- right-hand derivative 95
- Rolle's theorem 101
- sandwich principle 23, 63
- sequence 17
- series 36
- sign function 64
- singleton set 11
- singular integral 142
- singularity 142
- square root 71, 75
- square subsequence 32
- strict inequality 23, 63
- strictly increasing
 - sequence 31
 - function 73
- subadditivity of modulus 8
- subsequence 31
- sum of series 37
- summation notation 37
- supremum 11
- taking limits in inequalities 23, 63
- Taylor series 115
- Taylor's theorem with remainder 115, 140
- term
 - of sequence 17
 - of series 37
- tests for series
 - alternating series 46
 - comparison 42
 - condensation 56
 - integral 151
 - non-null 42
 - nth root 56
 - ratio 44
- tests for singular integrals
 - comparison 146
- transitive law 3
- trichotomy law 3
- trigonometric functions
 - definition and basic properties of 83–7
 - differentiability of 105
- uniqueness of limits 23
- upper bound 10
- upper bound axiom 11
- upper integral 125
- upper sum 122
- W-condition 77
- W'-condition 103
- Weierstrass' theorem
 - on series of continuous functions 77
 - on series of differentiable functions 103